

BHARAT SCHOLL OF BANKING

VOLUME AND SURFACE AREAS

Q1. Surface area of a cube is 600 cm^2 . Find out the length of its diagonal.

- (a) $15\sqrt{3}$
- (b) $12\sqrt{3}$
- (c) $10\sqrt{3}$
- (d) $11\sqrt{3}$
- (e) None of these

S1. Ans.(c)

Sol. Surface area of a cube = $6 \times (\text{side})^2$

$$\therefore 6 \times (\text{side})^2 = 600$$

$$\Rightarrow (\text{Sides})^2 = 100$$

$$\Rightarrow \text{Side} = \sqrt{100} = 10 \text{ cm}$$

$$\therefore \text{Diagonal of the cube} = \sqrt{3} \times \text{side}$$

$$= \sqrt{3} \times 10 = 10\sqrt{3} \text{ cm.}$$

Q2. A roller is 120 cm long and has diameter 84 cm. If it takes 500 complete revolutions to level a play ground, then determine to cost of leveling at the rate of 30 paise per m^2 . (Use $\pi=22/7$)

- (a) Rs. 475.40
- (b) Rs. 375.45
- (c) Rs. 375.20
- (d) Rs. 475.20
- (e) None of these

S2. Ans.(d)

$$\text{Sol. } r = \frac{84}{2} \text{ cm} = \frac{21}{50} \text{ m,}$$

$$h = 120 \text{ cm} = \frac{120}{100} \text{ m} = \frac{6}{5} \text{ m}$$

The leveled area in one revolution of the roller

$$= \text{curved surface} = 2\pi rh$$

$$= 2 \times \frac{22}{7} \times \frac{21}{50} \times \frac{6}{5}$$

$$= \frac{396}{125} \text{ m}^2.$$

The levelled area in 500 revolutions

$$= \frac{396}{125} \times 500 = 1584 \text{ m}^2.$$

$$\text{The required cost of leveling} = \frac{30}{100} \times 1584$$

$$= \text{Rs. } 475.20$$

Q3. The capacity of a tank, in the form of a cylinder, is 6160 m^3 . If the diameter of its base is 28 m, find out the cost of painting its inner curved surface at the rate of Rs. 2.8 per m^2 . (Use $\pi=22/7$)

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- (a) 2464
- (b) 2664
- (c) 3064
- (d) 2864
- (e) None of these

S3. Ans.(a)

Sol. Radius of the base of the cylinder

$$= r = 14 \text{ m.}$$

h = Depth of the tank

Capacity = Volume of the tank

$$= \pi r^2 h = 6160 \text{ m}^3.$$

$$\text{or, } \frac{22}{7} \times 14 \times 14 \times h = 6160 \quad \therefore h = 10 \text{ m.}$$

$$T \text{ surface area} = 2\pi r h = 2 \times \frac{22}{7} \times 14 \times 10$$

$$= 880 \text{ m}^2$$

\therefore Cost of painting this curved surface

$$= 880 \times 2.80 = \text{Rs. } 2464$$

Q4. The ratio of total surface area to lateral surface area of a cylinder whose radius is 80 cm and height 20 cm, is:

- (a) 2 : 1
- (b) 3 : 1
- (c) 4 : 1
- (d) 5 : 1
- (e) None of these

S4. Ans.(d)

$$\text{Sol. } \frac{\text{Total surface area}}{\text{Lateral surface area}} = \frac{2\pi r h + 2\pi r^2}{2\pi r h}$$
$$= \frac{2\pi r(h+r)}{2\pi r h} = \frac{h+r}{h} = \frac{20+80}{20} = \frac{5}{1} = 5 : 1.$$

Q5. The diameter and slant height of a conical tomb are 20 m and 50 m, respectively. The cost of white washing its curved surface at the rate of 80 paise per m^2 is:

- (a) Rs. 2640
- (b) Rs. 1760
- (c) Rs. 26400
- (d) Rs. 17600
- (e) None of these

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S5. Ans.(d)

Sol. Curved surface of the tomb

$$= \pi r l = \frac{22}{7} \times 14 \times 50 = 22000 \text{ m}^2$$

∴ Cost of white washing

$$= 22000 \times 0.80 = \text{Rs. } 17600$$

Q6. The curved surface of a cylindrical pillar is 264 m^2 and its volume is 924 m^3 . Taking $\pi=22/7$, find out the ratio of its diameter to its height:

- (a) 7 : 6
- (b) 6 : 7
- (c) 3 : 7
- (d) 7 : 3
- (e) None of these

S6. Ans.(d)

Sol. Curved surface of a pillar = 264 m^2

$$\text{or, } 2\pi r h = 264 \text{ m}^2$$

$$\text{or, } r h = \frac{264 \times 7}{2 \times 22}$$

$$\therefore r h = 42 \text{ m}^2 \quad \dots(1)$$

Again, $\pi r^2 h = 924 \text{ m}^3$

$$r^2 h = \frac{924}{22} \times 7$$

$$\therefore r^2 h = 294 \quad \dots(2)$$

Dividing Equation (2) by Equation (1)

$$r = 7 \text{ m}$$

$$\therefore h = \frac{42}{7} = 6 \text{ m}$$

Hence, required ratio = $7 \times 2 : 6 = 7 : 3$

Q7. If the surface area of a sphere is 346.5 cm^2 , then its radius is [taking $\pi=22/7$]

- (a) 7 cm
- (b) 3.25 cm
- (c) 5.25 cm
- (d) 9 cm
- (e) None of these

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S7. Ans.(c)

Sol. Surface area of sphere = $4\pi r^2$

Now, according to the question,

$$4 \times \frac{22}{7} \times r^2 = 346.5$$

$$\Rightarrow 4 \times 22 \times r^2 = 346.5 \times 7$$

$$\Rightarrow r^2 = \frac{346.5 \times 7}{4 \times 22} = 27.5625$$

$$\Rightarrow r = \sqrt{27.5625} = 5.25 \text{ cm}$$

Q8. The base of a right prism is an equilateral triangle. If the lateral surface area and volume is 120 cm^2 and $40\sqrt{3} \text{ cm}^3$, respectively, then the side of base of the prism is:

- (a) 4 cm
- (b) 5 cm
- (c) 7 cm
- (d) 40 cm
- (e) None of these

S8. Ans.(a)

Sol. Lateral surface area of prism = $3 \times \text{side} \times \text{height}$

$$\therefore 3 \times \text{side} \times \text{height} = 120$$

$$\Rightarrow \text{Side} \times \text{height} = \frac{120}{3} = 40 \text{ cm}^2 \quad \dots(1)$$

Volume of prism = Area of base \times height

$$\Rightarrow 40\sqrt{3} = \frac{\sqrt{3}}{4} \times \text{side}^2 \times \text{height}$$

$$\Rightarrow \frac{40\sqrt{3} \times 4}{\sqrt{3}} = \text{side}^2 \times \text{height}$$

$$\therefore \text{side}^2 \times \text{height} = 160 \text{ cm}^3 \quad \dots(2)$$

Dividing equation (2) by (1), we get

$$\text{Side} = \frac{160}{40} = 4 \text{ cm}$$

Q9. If a right circular cone of height 24 cm has a volume of 1232 cm^3 , then the area (in cm^2) of curved surface is:

- (a) 550
- (b) 704
- (c) 924
- (d) 1254
- (e) None of these

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S9. Ans.(a)

Sol. Let, the radius of cone be r cm.

Now, according to the question,

$$\frac{1}{3} \times \frac{22}{7} \times r^2 \times 24 = 1232$$

$$\therefore r^2 = \frac{1232 \times 3 \times 7}{22 \times 24} = 49$$

$$\therefore r = \sqrt{49} = 7 \text{ cm}$$

$$\therefore \text{Area of the curved surface} = \pi r l = \pi r \sqrt{h^2 + r^2}$$

$$= \frac{22}{7} \times 7 \times \sqrt{24^2 + 7^2} = 22 \times 25 = 550 \text{ cm}^2$$

Q10. A semicircular sheet of metal of diameter 28 cm is bent into an open conical cup. The capacity of the cup (taking $\pi=22/7$) is:

- (a) 624.26 cm^3
- (b) 622.36 cm^3
- (c) 625.56 cm^3
- (d) 623.20 cm^3
- (e) None of these

S10. Ans.(b)

Sol. If the radius of the base of cup be r cm, then $2\pi r = \pi \times 14$

$$\Rightarrow r = 7 \text{ cm}$$

Slant height = 14 cm

$$\therefore \text{Height} = \sqrt{14^2 - 7^2} = \sqrt{21 \times 7} = 7\sqrt{3} \text{ cm}$$

$$\therefore \text{Capacity of cup} = \frac{1}{3} \pi r^2 h$$

$$= \frac{1}{3} \times \frac{22}{7} \times 7 \times 7 \times 7\sqrt{3} = 622.36 \text{ cm}^3.$$